Restricting the search space \(\{0, 1\}^n\) to the set of truth tables of “easy” Boolean functions on logarithmically many variables, as well as using some known hardness-randomness tradeoffs, we establish a number of results relating the complexity of exponential-time and probabilistic polynomial-time complexity classes. In particular, we show that $\text{NEXP} \subset \text{P/poly} \iff \text{NEXP} = \text{MA}$; this can be interpreted as saying that no derandomization of $\text{MA}$ (and, hence, of promise-$\text{BPP}$) is possible unless $\text{NEXP}$ contains a hard Boolean function. We also prove several downward closure results for $\text{ZPP}$, $\text{RP}$, $\text{BPP}$, and $\text{MA}$; e.g., we show $\text{EXP} = \text{BPP} \iff \text{EE} = \text{BPE}$, where $\text{EE}$ is the double-exponential time class and $\text{BPE}$ is the exponential-time analogue of $\text{BPP}$. 