

**Lecture 4. Part 1. Nov. 12, 2014.** Fibration sequences.

**Lecture 4. Part 2. Nov. 12, 2014. 0-11min** Fibration sequences.

**11-16min** Fiberwise weak equivalences.

**16-24min** The `fmap` and its fibers.

**Lecture 5. Part 1. Nov. 19, 2014. 0-5min** More on fibration sequences.

**5-12min** h-levels of types.

**12-15min** h-levels of functions.

**15-24min** h-levels in classical mathematics.

**24-30min** h-levels of functions cont.

**30-33min** h-levels of maponpaths and some other special cases of functions.

**33-43min** Types of h-level 1 and general remarks.

**43-47min** A contractible type is a proposition.

**47-50min** h-level  $n$  implies h-level  $n+1$ .

**50-55min** More on types of h-level 1. Introducing `hProp`.

**55-the end of the file** Resizing rule. Impredicativity.

**Lecture 5.Part 2. Nov. 19, 2014. 0-6.5min** The difference between `bool` and `hProp`.

**6.5-15min** Canonicity for `bool`. Weak canonicity. Canonicity for `nat`.

**15-17.5min** Univalent canonicity conjecture for `nat`.

**17.5-23.5min** More on weak canonicity.

**23.5-27.5min** Why there is no canonicity after adding the axiom of excluded middle.

**27.5-33min** More discussion on modeling `Coq` in `Coq`.

**33-34min** About proof of canonicity and its conditionality.

**34-the end of the file** Meta-theories for proofs of relative consistency.

**Lecture 6. Part 1. Nov. 25, 2014. 0-4min** Univalence axiom - definition.

**4-10.5min** Connection of the univalence axiom to Church's extensionality.

**10.5-13:30min** Function extensionality for morphisms to the empty type is introduced and discussed.

**13:30-17min** Connection between extensionality and canonicity for the identity types.

**17-24min** Connections between univalence and constructive extensionality. Cubical type theory.

**24-26min** Uses of function extensionality for functions to the empty type. More properties of inclusions. (Note: in the present version of the `UniMath` the function extensionality for the empty type was moved lower to the beginning of the file `uu0c.v`)

**26-27:30min** The definition of a set. Elementary facts.

**27:30-43min** Complements. The union of the complement to an object with the point. Isolated points. Types with decidable equality. Some discussion about  $\text{weq } X$  when  $X$  is given with an isolated point  $x$ . Application to the set of automorphisms of a finite set.

**43min-51min** Theorem that a type with decidable equality is a set. Discussing why equality in circle is undecidable.

**51-53.5min** More properties of h-levels related to disjoint unions and complements.

**53.5-55min** Definition of decidable propositions. Decidable inclusions.

**55-to the end of the file** General function extensionality is introduced. Short discussion of the eta-conversion.

**Lecture 6. Part 2. Nov. 25, 2014. 0-4.5min** Discussion of function extensionality and some simple consequences.

**4.5-7min** “Impredicativity” property of h-levels.

**7-10.5min** Different meanings of the word “impredicativity”. The “size” of the excluded middle axiom as an example.

**10.5-13min** About the fact that all types whose name starts with “is” are propositions. Weak equivalences between weak equivalences. How these assertions will look in the cubical type theory?

**13-15min** Some remarks about whether it is good to have more models or fewer models.

**15- 17.5min** The theorem about the auto-equivalences of a type with a distinguished isolated point that was mentioned earlier. Decomposition of permutations into transpositions. Why did I want to formalize such things?

**17.5min** The course reached the end of `uu0.v` (that is now `uu0a`, `uu0b`, `uu0c`, `uu0d`).

**17.5-23min** Discussion of the structure of the rest of the library.

**23-27.5** Example of the absolute value of the integral part of a rational number as a function that is constructed using set-quotients and other univalent ideas but which computes  $(|\text{int}(10/(-3))| = 4)$

**27.5-29min** Further comments on the structure of the library.

**29-34min** About the formalization of the category of simplicial sets and how from there one can go to the formalization of the classical homotopy theory.

**34-end of the file** A question about the pre-category  $\Delta$ .