

# PETER SARNAK

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LETTERS, LECTURES AND NOTES<sup>†</sup> (can all be found on:)

<sup>†</sup> <http://www.math.princeton.edu/sarnak/>

- Notes with Paul Cohen on the trace formula (analytic continuation of Eisenstein series) (1980).
- Letter to E. Bombieri on symplectic pairings and  $L$ -functions (2001).
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