Both estimates (2.13) and (4.2) are incorrect: the right hand side is missing a factor r^{-1} . The correct estimate is

$$\left|I(z,r) - I(y,r)\right| \le C \left[\left(W_{r/8}^{4r}(x_1)\right)^{1/2} + \left(W_{r/8}^{4r}(x_2)\right)^{1/2} \right] \frac{|z-y|}{r} \qquad \forall z, y \in [x_1, x_2].$$
(1)

This estimate is in fact the one which is invariant under the rescaling $u_r(x) := u(rx)$, which is the rescaling used in the proof to reduce the statement to the case r = 1. The mistake is no consequence for the rest of the paper because in fact the estimate is used when r = 1 in all the subsequent arguments.

Moreover, in the last two displayed equations of Section 4 the square root is missing on the right hand sides. The correct estimates are

$$\partial_v I(x,1) \le C(\sqrt{W(x_1)} + \sqrt{W(x_2)}) \qquad \forall x \in [x_1, x_2]$$
$$|\partial_v I(x,1)| \le C(\sqrt{W(x_1)} + \sqrt{W(x_2)}) \qquad \forall x \in [x_1, x_2].$$