

abstract

COMPUTER SCIENCE/DISCRETE MATH, II
Topic:

Speaker:

Affiliation:

Date:

Time/Room:

Khot formulated in 2002 the "Unique Games Conjectures" stating that, for any $\epsilon > 0$, given a system of constraints of a certain form, and the promise that there is an assignment that satisfies a $1-\epsilon$ fraction of constraints, it is intractable to find a solution that satisfies even an ϵ fraction of constraints. Recent work has shown that the conjecture implies a number of very strong inapproximability results, including tight results for Max Cut and Vertex Cover. Generalizations of the conjecture to the case of sub-constant ϵ have also been considered, and shown to imply inapproximability results for Sparsest Cut and other problems.

We show that a strong generalization of the conjecture to sub-constant ϵ fails.

Namely, we show that, given a system of constraints and the promise that there is an assignment that satisfies a $1-1/O(\log n)$ fraction of constraints, we can find in polynomial time an assignment that satisfies 99% of the constraints.

Feige and Reichman have shown that the problem of finding a solution that maximizes the number of satisfied constraints is hard to approximate within a $2^{\{(\log n)^{.99}\}}$ factor, and so our work shows that the promise that the system is almost satisfiable changes its approximability a lot.