

abstract

Joint IAS-PU Symplectic Geometry Seminar
Topic:

Speaker:

Affiliation:

Date:

Time/Room:

Fix a metric (Riemannian or Finsler) on a compact manifold M . The critical points of the length function on the free loop space LM of M are the closed geodesics on M . Filtration by the length function gives a link between the geometry of closed geodesics, and the algebraic structure given by the Chas-Sullivan product on the homology of LM and the "dual" loop cohomology product.

If X is a homology class on LM , the "minimax" critical level $Cr(X)$ is a critical value of the length function. Gromov proved that if M is simply connected, there are positive constants k and K so that for every homology class X of degree $\geq \dim(M)$ on LM ,

$$k \deg(X) \leq Cr(X) \leq K \deg(X).$$

When M is a sphere, we prove there are positive constants a and b so that for every homology class X on LM ,

$$a \deg(X) - b \leq Cr(X) \leq a \deg(X) + b.$$

There are interesting consequences for the length spectrum.

Mark Goresky and Hans-Bert Rademacher are collaborators.