

## abstract

[Video of this lecture](#) COMPUTER SCIENCE/DISCRETE MATH II

Topic:

Speaker:

Affiliation:

Date:

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We consider the problem of approximately solving a system of homogeneous linear equations over reals, where each equation contains at most three variables. Since the all-zero assignment always satisfies all the equations exactly, we restrict the assignments to be "non-trivial". We prove the hardness of the following problem: Distinguish whether there is a non-trivial assignment that satisfies  $1-\delta$  fraction of the equations or every non-trivial assignment fails to satisfy a constant fraction of the equations with a "margin" of  $\sqrt{\delta}$ . The hardness result matches the performance of a natural semi-definite programming-based algorithm. To prove our result, we develop linearity and dictatorship testing procedures for functions  $f: \mathbb{R}^n \rightarrow \mathbb{R}$  over a Gaussian space, which could be of independent interest. Our research is motivated by a possible approach to proving the Unique Games Conjecture