

## abstract

ARITHMETIC COMBINATORICS

Topic:

Speaker:

Affiliation:

Date:

Time/Room:

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For a probability distribution  $X$  over a finite set, let  $D(X)$  denote the  $L_2$ -distance of  $X$  from the uniform distribution. Let  $X, Y$  be probability distributions over the finite group  $G$  and let  $Z$  be their  $G$ -convolution. Inspired by recent work of Gowers, we prove that

$$(*) \quad D(Z) \leq \sqrt{n/m} \, D(X) \, D(Y),$$

where  $n=|G|$  and  $m$  is the minimum degree of nontrivial real representations of  $G$ .

We deduce several corollaries on product growth of subsets of  $G$ , including improved and generalized versions of Gowers' result on the solvability of the equation  $xy = z$  in given subsets of  $G$ . One of the corollaries to  $(*)$  gives a best possible answer to a question by Venkatesh and Green on the product growth of subsets of  $SL_2(q)$ . Applications to Helfgott-type diameter and mixing arguments follow as well.

A number of applications to the area of "bounded generation" in group theory have been found. One such application:

Every finite quasisimple group of Lie type of characteristic  $p$  can be written as the product of five of its Sylow  $p$ -subgroups.

This improves and simplifies a previous result which served as an ingredient in the proof of Serre's conjecture on the topology of profinite groups (Nikolov-Segal) and the recent result that all finite quasisimple groups of Lie type have expander generators (Kassabov - Lubotzky - Nikolov).

Joint work with Nikolay Nikolov and Laszlo Pyber