

HIGH-RESOLUTION PRINTER GRAPHICS

BY MARK BRIDGER AND MARK GORESKY

You can address the individual dots used to generate dot-matrix characters

ONE OF THE GREATEST frustrations in doing graphics on a microcomputer is the rather low resolution of the usual microcomputer monitor. The standard IBM Personal Computer color-graphics adapter and monitor display a maximum screen size of 640 by 200 pixels (picture elements); other computers and configurations do somewhat better, perhaps as much as 720 by 350 pixels. It is difficult to draw horizontal lines fast enough to keep the image from flickering. And there are limits to the amount of screen memory available on standard graphics boards.

Many dot-matrix printers are capable of printing individual dots at a much higher resolution than the typical CRT (cathode-ray tube) screen can display them. The Epson FX-80 and the IBM graphics printer are capable, for example, of printing 240 dots per inch horizontally (1920 dots per line) and 216 dots per inch vertically—the latter by printing a line of graphics, advancing the paper one-third of a dot, printing another “interlaced” line of graphics, etc. Other printers can perform similar feats. To use this

capability you need to figure out how to “fire the pins,” and you need enough extra memory to record where all the dots are to go. This article will show you how to draw some lines and curves on your printer with a resolution of up to 1600 by 640 dots.

SETTING UP THE “PRINTER SCREEN”

The first problem is memory. If you think of a dot as being either on or off, to use an analogy with the screen display, then encoding 1600 by 640 dots, or 1,024,000 points, requires that many *bits* of information. If you divide by 8 to convert bits to bytes, then the process requires 128,000 bytes, or nearly 128K bytes of memory. Somehow, you must set aside that much memory to record this image. Unfortunately, this is not easily done in BASIC, so we must look elsewhere.

The most widely used microcomputer language that allows fencing off this much memory is Pascal, and because Turbo Pascal lets you point to nearly all available memory without having to give explicit addresses,

it is the easiest language to use.

Let's set up two 64K-byte memory areas that represent the even lines and the odd lines of a picture. Each of these areas is represented by the following Pascal data type:

```
Type data__type = array[0..1599,
0..39] of char;
```

This type of variable is a doubly indexed 1600 by 40 array of characters; since one byte represents each character, this multiplies to about 64K bytes.

Now let's declare the variables that are to reserve this space:

```
Var Evenmap, Oddmap:
^data__type;
```

(continued)

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The “^” defines a pointer. When you actually create these variables during program execution, using the command **New**, the computer sets aside two blocks of free memory and automatically reserves them for your use. Each of the variables **Evenmap** and **Oddmap** “points” to the beginning of one of these blocks, and you need never concern yourself with exactly where in memory these blocks reside.

HOW A DOT-MATRIX PRINTER DRAWS DOTS

The print head of a dot-matrix printer normally has seven or more wires, arranged vertically; the most common

number is nine. (Eight are used to draw most of the characters, while the ninth is used to draw the bottoms of the g and y characters and to underline.) When typing letters, the printer receives the ASCII code of the character—a number between 0 and 255. As the print head moves across the page, it extends certain wires, depending on the pattern stored in the printer’s memory for that character, and the head strikes them against the paper. Usually from 9 to 12 such columns of dots are needed to make a character.

You want to be able to tell the printer directly which wires to fire; in

other words, you want to bypass that part of the printer’s memory that stores the patterns for the printing of usual characters (letters, numbers, etc.)—you want to do *bit-mapped* graphics. Most printers support this; it is usually called graphics mode. Let’s try to address a particular dot on the page.

First, since the wires on the print head are not that close together, you can make use of tiny partial linefeeds to double the number of vertical dots. Table 1 contains a diagram of how it works. The characters represent dot positions on the page; the 1s represent the dots that you actually want to draw and the 0s represent the dot positions you want to skip. To get maximum resolution, you want the dots to be as close to each other as possible, both horizontally and vertically. Getting them close horizontally is accomplished by means of a simple printer command. To get them close vertically, you must divide the picture into the even rows (0, 2, 4, etc.) and the odd rows (1, 3, 5, etc.), as shown in table 2.

When the printer is in graphics mode, the printer prints, for each byte you send it, any pattern of eight vertical dots you specify. The strategy in table 2 is to do the following:

1. Send the printer the 10 bytes that specify the 10 columns represented by the even rows.
2. Instruct the printer to do a carriage return plus a linefeed of one-half a vertical dot.
3. Send the printer the 10 bytes that specify the 10 columns represented by the odd rows.
4. Instruct the printer to do a carriage return plus a linefeed of 7½ vertical dots, preparing it to draw more sets of even and odd rows if there are any.

In more ambitious applications you can have as many as 1600 columns across instead of just these 10. The array pointers **Evenmap** and **Oddmap** store this information for the printer. Each represents 1600 columns; each column is 40 bytes or 320 dots high. Looked at another way, there are 320

(continued)

Table 1: This table shows the dot positions on the page. The 1s represent dots that you actually want to draw; the 0s, dot positions you want to skip over.

0	1	0	0	0	0	0	0	0	0	0
1	0	1	0	0	0	0	0	0	0	0
2	0	0	1	0	0	0	0	0	0	0
3	0	0	0	1	0	0	0	0	0	0
4	0	0	0	0	1	0	0	0	0	0
5	0	0	0	0	0	1	0	0	0	0
6	0	0	0	0	0	0	1	0	0	0
7	0	0	0	0	0	0	0	1	0	0
8	0	0	0	0	0	0	0	0	1	0
9	0	0	0	0	0	0	0	0	0	1
10	0	0	0	0	0	0	0	0	0	1
11	0	0	0	0	0	0	0	0	1	0
12	0	0	0	0	0	0	0	1	0	0
13	0	0	0	0	0	0	1	0	0	0
14	0	0	0	0	0	1	0	0	0	0
15	0	0	0	0	1	0	0	0	0	0

Table 2: This table shows the distribution of the various print dot positions between even and odd rows.

Even:	0	1	0	0	0	0	0	0	0	0	Odd:											
											1	0	1	0	0	0	0	0	0	0	0	
	2	0	0	1	0	0	0	0	0	0	3	0	0	0	1	0	0	0	0	0	0	
	4	0	0	0	0	1	0	0	0	0	5	0	0	0	0	0	1	0	0	0	0	
	6	0	0	0	0	0	0	1	0	0	7	0	0	0	0	0	0	0	1	0	0	
	8	0	0	0	0	0	0	0	0	1	0	9	0	0	0	0	0	0	0	0	0	1
	10	0	0	0	0	0	0	0	0	1	11	0	0	0	0	0	0	0	0	1	0	
	12	0	0	0	0	0	0	0	1	0	0	13	0	0	0	0	0	0	1	0	0	0
	14	0	0	0	0	0	1	0	0	0	0	15	0	0	0	0	1	0	0	0	0	0

even rows and 320 odd rows. Each row is 1600 dots wide, and the printer will print eight even or eight odd rows in each pass. Note that these rows form a natural unit totaling 16 rows; let's call such a unit a printer line.

HOW TO LOCATE A DOT ON THE PAGE

Let's write a procedure—Pset(x,y,color)—that draws a point of coordinates x and y in the proper place in one of the two arrays. The coordinates x and y denote the point's column and row (measured from the upper left-hand corner), respectively. The variable color can be equal to either 0 or 1: 0 means erase any point existing at that location; 1 means insert a point there. [Editor's note: All programs shown here are available for downloading on BYTEnet Listings. Before November 1 call (617) 861-9774. Afterwards, call (617) 861-9764.]

See listing 1 for the procedure Pset. Start at the line that reads color := color mod 2. First the procedure ensures that color is in the correct range by applying a mod 2 to it. (When K and N are whole numbers, K mod N finds the remainder you get when you divide K by N. When you divide by 2, you can get a remainder of only 0 or 1, depending on whether K is even or odd, respectively.) Next, you determine which printer line you're in by dividing the row number by 16 (y div 16). When you know this line number, you can determine which vertical dot within that line you're in: this is height. Finally, y mod 2 tells you whether your dot is in an even or an odd row.

For example, suppose you want to print a dot in column 1173, row 554. Then x equals 1173 and y equals 554. 554 div 16 equals 34, so you are in the 34th printer line. 554 mod 16 is 10 and 10 div 2 is 5, so the height of the dot within the printer line is 5; since 554 is even, you are in the array pointed to by Evenmap. The program now calls on the procedure Change to insert this point into the correct position in memory.

The problem now, and the reason Change is so complicated, is that

(continued)

Listing 1: Epson FX-80 procedures in disk file Printpak.pas.

```

const
  across = 1599;    (** replace with 1249 for Prowriter **)
  down   = 39;

type
  data__type = array[0..across, 0..down] of char;
  mask__array = array[0..7] of byte;

var
  Evenmap, Oddmap: ^data__type;
  M, R: mask__array;

procedure Init__mem;
var I,J: integer;
begin
  new(Evenmap); new(Oddmap);    {sets aside space in memory for arrays}
  for J := 0 to down do
    for I := 0 to across do
      begin
        oddmap^[I,J] := chr(0);    {initializes both arrays}
        evenmap^[I,J] := chr(0)    {all bytes = 0}
      end
    end;
  {Init__mem}

procedure Printout;    {Output to EPSON FX-type printer.}
var n_lo, n_hi:byte;    {See listing 2 for Prowriter Printout.}
    i,j : integer;
begin {Printout}
  n_hi:= (across + 1) div 256;    {Part of number of graphics bytes coming}
  n_lo:= (across + 1) mod 256;    {Rest of number of graphics bytes coming}
  for J := 0 to 39 do
    begin
      write (Lst,chr(27),'Z',chr(n_lo),chr(n_hi));
      {Enter graphics mode; give # bytes coming}
      for I := 0 to across do write(Lst, evenmap^[I,J]); {print even row}
      write(Lst,chr(13));    {carriage return}
      write(Lst, chr(27),'3',chr(1));    {set linefeed for 1/3 dot down}
      write(Lst, chr(10));    {do linefeed}
      write (Lst, chr(27),'Z',chr(n_lo),chr(n_hi));    {graphics mode again}
      for I := 0 to across do
        write (Lst, oddmap^[I,J]);    {print odd row}
        write(Lst, chr(13));    {carriage return}
        write(Lst,chr(27),'3',chr(22));    {start next line 7 1/3 dots down}
        write(Lst, chr(10));    {linefeed}
      end
    end;
  {Printout}

procedure PixelMasks;
var I: integer;
begin
  M[7] := 1;
  for I := 6 downto 0 do M[I] := 2*M[I + 1];
  for I := 0 to 7 do R[I] := 255 - M[I]
end; {Pixelmasks}

procedure Change (var Char__byte: char; color, height:integer);
{changes given byte from present value to given value = color}
var old: integer;
begin
  Old := ord(Char__byte);
  case color of
    1: old := old OR M[height];    {insert set bit in correct place}
    0: old := old AND R[height]    {using appropriate pixel masks}
  end;
end;

```

(continued)

```

(*****
For the Prowriter these last two lines should be replaced by
1: old := old OR M[7 - height];
2: old := old AND R[7 - height]  {See text for details.}
***** )
end;
Char_byte := chr(old)
end; {Change}

procedure Pset (x,y,color : integer);
{Writes the dot at position (x,y) into memory arrays}
var l,line,height : integer;
begin {Pset}
  Plot(x * 2 div 5, y * 5 div 16, white); {draw dot on screen}
  { *****
  This multiplies x by the ratio of screen width to printer width,
  multiplies y by the ratio of screen height to printer height.

  For the Prowriter this last line should be replaced by:

  Plot(x div 2, y * 5 div 16, white);
  ***** }

  color := color mod 2;
  Line := Y div 16;           {vertical position of pixel consists of a line}
  height := (Y mod 16) div 2; {number between 0 and down; and a height }
                                {between 0 and 15, divided into}
                                {even-odd groups}

  if y mod 2 = 0 then change(evenmap^[x,line],color,height)
    else change(oddmap^[x,line],color,height)

end; {Pset}

```

Listing 2: Printout procedure for Prowriter.

```

procedure Printout;           {for Prowriter}
var wrd : packed array [1..4] of char;
    a,b,i,j,k : integer;
begin {Printout}
  writeln (lpt1, '          '); {clear printer buffer}
  writeln (lpt1, '          '); { = 50 bytes}
  writeln (lpt1);              { + carriage return}
  a := across + 1; l := 4;     {a = number of graphics bytes}
  repeat
    b := a mod 10; a := a div 10; {get next digit (= b)}
    wrd [l] := chr(b + ord('0')); {insert as a character in string: wrd}
    l := l - 1
  until l = 0;                 {wrd = digits of across}
  writeln (lpt1, chr(27), 'P'); {set pitch for proportional spacing —
                                the highest horizontal density}

  for J := 0 to down do
  begin
    write (lpt1, chr(27), 'S', wrd); {enter graphics mode}
    for l := 0 to across do
      write (lpt1, evenmap^[l,J]); {print even rows}
    writeln (lpt1, chr(27), 'T', '01'); {start next line 1/2 dot down}
    write (lpt1, chr(27), 'S', wrd); {graphics mode again}
    for l := 0 to across do
      write (lpt1, oddmap^[l,J]); {print odd rows}
    writeln (lpt1, chr(27), 'T', '15'); {start next line 7/2 dots down}
  end
end; {Printout}

```

turning on a point involves changing a single bit within a byte. Computers are generally not equipped to do this easily. Remember that each byte controls eight vertical dots, and you want to change *only one* of them. This is most quickly done with bit masks and the logical operations AND and OR. See the text box on bit manipulation, "Bits AND/OR Pieces," on page 225. (Note that in the PixelMasks procedure, the leftmost bit in a byte is called the zeroth bit, while the rightmost bit is the seventh.)

If you want to insert a 1 in the third bit, you use the mask M[height], where height equals 3, with the logical OR operation. The code that inserts this 1 into the byte Old is simply:

Old := Old OR M[height]

M[height] is a byte made up of all zeros except for a 1 in bit height. If Old is 01000010 and height is 3, then Old becomes the byte (01000010 OR 00010000) = 01010010.

If you want to insert a 0 into this same byte, you use the mask R[height] together with the logical AND operation:

Old := Old AND R[height]

Here, R[height] is a byte made up of 1s except for a 0 in bit height. If Old is 01111101 and height is 7, then Old becomes the byte (01111101 AND 11111110) = 01111100.

Note that you write to printers using Pascal's Write and Writeln procedures, and these procedures expect to be given a character. This is why you should set up your arrays as character arrays and why the last command in the Change procedure converts the byte into a character.

SOME PRINTER DIFFERENCES

The eight vertically arranged print pins on most printers correspond to the eight bits in a byte. On the Epson FX-80 and many other printers, the high-order bits—those in the left half of the byte—correspond to the upper pins; the low-order, or rightmost, bits correspond to the lower pins. Thus, the byte 10000010 causes the top pin and the next-to-the-bottom pin to

make dots on the paper. On the other hand, for the Prowriter and several other printers, the exact opposite is true—the *leftmost* bit causes the *bottom* pin to fire. Thus, if you want to insert a 1 in the third bit for a Prowriter, you OR with M[7-height] where height equals 3. To avoid confusion we have indicated the corrections necessary to handle the Prowriter properly (see listing 2). If you have a different printer, you should check your manual for the correct pin assignments. (The Prism printer, for example, uses only seven pins.)

Another important difference between printers is in how close you are allowed to print the dots horizontally and vertically. In the Epson quadruple-density graphics mode, available only on the FX, RX, and IBM models, the printer prints 240 dots per inch or 1920 dots across an 8-inch page. Because of restrictions on the size of arrays (64K-byte maximum), the examples in this article draw only 1600 dots. (We can draw more, but at the expense of some vertical rows.) The older Epson MX prints only 960 dots across the page. For the Prowriter, the highest density possible is in proportional mode, where you can get 160 dots per inch or 1280 per line—we use 1250 in our examples.

Each dot on a dot-matrix printer is approximately 1/72 inch in diameter. The Epson FX-80 permits linefeeds of 1/3 dot, which results in a theoretical vertical density of 216 dots per inch. The Prowriter allows 1/2-dot linefeeds, or a vertical density of 144 dots per inch. In the examples in this article, we use the Epson 1/3-dot linefeeds as if they were 1/2-dot; this works fine, undoubtedly due to the inherent inaccuracy of paper advance.

Once again, you must consult your printer manual if you have a different printer. The Prism does not seem to support fractional linefeeds at all, while the Mannesmann Tally achieves them by raising or lowering the actual print head 1/2 dot.

ECHOING ON THE SCREEN

We now have the complete setup for drawing a dot in "printer" memory.

Returning to listing 1, note the call to the procedure Plot. Plot is a Turbo Pascal procedure that draws a dot on the actual screen for each point you draw in memory. However, the scale for the printer is different from the scale for the screen: 1600 by 640 dots for the printer (1250 by 640 dots for the Prowriter) versus 640 by 200 dots (pixels) for the screen. For the Epson

FX-80 you rescale by multiplying the column and row, respectively, by 640/1600 (2/5) and 200/640 (5/16). For the Prowriter you multiply by 640/1250 (approximately 1/2) and 200/640 (5/16). Since real-number multiplication is time-consuming (unless you have an 8087 chip) and since Plot requires integer parameters anyway, you

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BITS AND/OR PIECES

Suppose you have two bytes, each represented as eight binary bits: Byte1 = 10111010 and Byte2 = 00110011. To make calculation simpler later on, let's call the first bit on the left of each byte the zeroth bit; the next is the first, then the second, etc. Thus, the zeroth bit of Byte1 is 1, the first is 0, and the seventh, or rightmost, bit is 0. When you OR Byte1 and Byte2 together, you produce a new byte, Byte3. If either of the corresponding bits, for example the zeroth bits of Byte1 and Byte2, is a 1, then you make the corresponding bit of Byte3 a 1; otherwise, it is a 0. Thus, the zeroth bit of Byte3 is a 1 since Byte1 has a 1 in the zeroth position. The first bit of Byte3 is a 0 since neither Byte1 nor Byte2 has a 1 in that position.

```
Byte1 = 1 0 1 1 1 0 1 0
Byte2 = 0 0 1 1 0 0 1 1
Byte3 = 1 0 1 1 1 0 1 1
Byte3 = Byte1 OR Byte2 =
      10111011.
```

If you perform an AND on the two bytes, the process is similar, except that you put a 1 in Byte3 only if *both* corresponding bits are 1. Let's let Byte4 = Byte1 AND Byte2.

```
Byte1 = 1 0 1 1 1 0 1 0
Byte2 = 0 0 1 1 0 0 1 1
Byte4 = 0 0 1 1 0 0 1 0
Byte4 = Byte1 AND Byte2 =
      00110010
```

Suppose now that you have a byte B = 10011001 and you want to change the second bit from a 0 to a 1. If you have a byte M2 that is all 0s except for a 1 in this second position (i.e., third place from the left), then you can execute

```
B OR M2 = 10011001 OR 00100000
      = 10111001
```

This accomplishes your purpose. You need eight different masks of this type to handle each possible bit position. Note that M2 = 00100000 (binary) = 20 (hexadecimal) = 32 (decimal); also, 32 = 2⁽⁷⁻²⁾. All other such masks are powers of 2 also. This explains how M, the array of eight different pixel masks, is constructed in the procedure PixelMasks (see listing 1).

To turn off the fourth bit of B (i.e., change it from a 1 to a 0), you can AND it with a byte R4 that is all 1s except for a 0 in the fourth position (the reverse type of mask from M2):

```
B AND R4 = 10011001 AND 11110111
      = 10010001
```

In this case R4 = 11110111 (binary) = F7 (hexadecimal) = 247 (decimal). The procedure PixelMasks also constructs the array R of eight different reverse masks. The relation between the masks of the two types is easy to see. For example, consider M[3] = 00010000 = 16, and R[3] = 11101111 = 239. Then R[3] = 11101111 = 11111111 - M[3] = 255 - M[3]

Thus, you get the reverse pixel masks from the normal pixel masks by subtracting the normal ones from 255.

One great advantage of pixel masks is that they are fast. Once created, you can use them over and over without any time-consuming computation. You can use pixel masks in regular screen graphics also; if you use color, you will need several other sets of masks that do two bits at a time, since a choice of one out of four colors requires two bits.

can do this quite neatly using integer multiplication and div:

```
Plot(x * 2 div 5, y * 5 div 16, white)
```

For the Prowriter:

```
Plot(x div 2, y * 5 div 16, white)
```

This is still somewhat wasteful since it draws some dots on top of others, but it is sufficient for this example.

HOW TO PRINT THE DOTS

In theory all we have to do is send these bytes to the printer. However, many printers are fussy and don't like to be in graphics mode—in fact, they'll only stay there for one line at a time. Furthermore, each time you invoke graphics mode you have to tell them how many graphics bytes to expect on that line; if you send them more, they start printing regular characters.

Let's do a brief rundown on the Epson FX-80 graphics Printout procedure (see listing 1). Lst is Turbo Pascal's name for the printer. The Epson FX-80 instruction to enter quadruple-density graphics mode is Escape (chr(27)) followed by Z (on the MX, replace Z with L). Then the

printer needs to receive the number of graphics bytes it should expect as a sequence of two characters, which are determined as follows:

```
Byte #1 = "n_lo"
          (# of bytes mod 256)
Byte #2 = "n_hi"
          (# of bytes div 256)
```

(This information should be easy to obtain from your printer manual under "Graphics Mode.")

Procedure Printout has two nested loops; the big one controls the printer lines, while the smaller sends out the character bytes within each printer line. Recall that a printer line consists of one even and one odd group of 1600 bytes. For each of these we must, as just mentioned, reenter graphics mode and give the byte count. The command write(Lst, chr(13)) is simply a carriage return.

The only other lines of interest are the paperfeeds. The Epson FX-80 won't do a linefeed of 1/2 dot but rather works in multiples of 1/3 dot. Since even Epson disclaims any great accuracy for such a tiny linefeed, we tried various combinations such as 1/3

and 7/3, 2/3 and 7/3, etc. The best image seemed to result from using 1/3 and 7/3 (22/3).

Now let's take a look at the Prowriter graphics Printout procedure (see listing 2), since the Prowriter works a little differently. First, you should clear out the 50-byte printer buffer by writing 50 blanks—we've never seen the necessity of this, but it is suggested as a precaution. Next, you should report the number of graphics bytes the printer is to expect (= across + 1) by sending a string whose characters are the *decimal* digits of this number. These are computed by the small loop (from a: = across + 1 through until l = 0;). The rest of the code is the same as the Epson FX-80's except for the different printer instructions (escape sequences).

THE TESTCURVE PROGRAM

To demonstrate how these procedures work, listing 3 contains a driver program that sketches the simple parabola $y = x*x$ (see figure 1). The heart of this program is the procedure Plotcurve, which illustrates the scaling and coordinate manipulation necessary to draw "computer pictures." Since the origin is in the upper left-hand corner and the y -coordinate is measured downward, you are essentially plotting $y = 639 - (x - 25)*(x - 25)$. x should go from 0 to 50; since the width of the screen is across (1599 or 1249), you round across to the nearest 50 (width: = across - (across mod 50)) and let l go from 0 to width. The scale factor scaler is width/50 and x equals $l/scaler$ or $(l/width)*50$. Thus, when l equals 0, x is 0; when l equals width, x is 50. Then you use Pset to graph your points:

```
Pset(l, trunc(639 - (l/scaler - 25)*
(l/scaler - 25)), 1)
```

Note that you must truncate (trunc) since Pset requires integer parameters.

CONNECTING THE DOTS

The procedure Plotcurve draws a curve by computing each point sepa-

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Listing 3: Program to test printing procedures. It draws a parabola: $y = x*x$. Note the \$! directive to include the routines in Printpak.pas (see listing 1).

```
Program Testcurve;
{$! printpak.pas}      {Include printer procedures listed above.}
var ch: char;

Procedure Plotcurve;
var l, width: integer;
    scaler: real;
begin {Plotcurve}
    width: = across - (across mod 50);
    scaler: = width/50;
    for l: = 0 to width do
        Pset(l, trunc(639 - (l/scaler - 25)*(l/scaler - 25)), 1)
    end; {Plotcurve}
begin {Testcurve}
    Init_mem;
    PixelMasks;
    HiRes; HiResColor(7); {draw in 640- by 200-dot mode}
    Plotcurve;
    write('Continue (y/n)? ');
    readln(ch);
    if ch = 'y' then Printout;
    TextMode(BW80)
end. {Testcurve}
```

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rately and then plotting it. Although this sufficed for a simple demonstration, it has two major shortcomings. First, it can skip points. For example, suppose y equals 5 when x is 1, and y equals 10 when x is 2. Then there is a vertical gap of four dots between

the points (1,5) and (2,10). (This didn't happen on the parabola graphic because x went from 0 to 50 in 1599 steps, so each step represented an x change of about 0.03. Thus, even at the steepest part of the curve, y

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Listing 4: Bresenham's line-drawing algorithm. (The Pascal implementation is courtesy of Professor Richard Rasala of Northeastern University.)

```

Procedure Pixel_Line(x1,y1,x2,y2:integer);
var x, y, z, a, b, dx, dy, d, deltap, delta: integer;
begin
  dx := abs(x2 - x1);
  dy := abs(y2 - y1);
  If dy <= dx then {Slope <= 1}
  begin
    x := x1; {initialize x}
    y := y1; {initialize y}
    z := x2; {set sentinel in x-direction}
    {Now set x-increment}
    If x1 <= x2
      then a := 1 {x increases}
      else a := -1; {x decreases}
    {Now set y-increment}
    If y1 <= y2
      then b := 1 {y increases}
      else b := -1; {y decreases}
    {Initialize decision function and its deltas}
    deltap := dy + dy;
    d := deltap - dx;
    delta := d - dx;
    {Locate and plot points}
    Pset(x,y,1); {First point}
    while x <> z do begin
      x := x + a;
      if d < 0
        then d := d + deltap
        else begin
          y := y + b;
          d := d + delta;
        end; {else}
      Pset(x,y,1);
    end {while}
  end {Case: if dy <= dx}
else {dx <= dy so view x as a function of y}
begin
  y := y1; {initialize y}
  x := x1; {initialize x}
  z := y2; {set sentinel in y-direction}
  {Now set y-increment}
  If y1 <= y2
    then a := 1 {y increases}
    else a := -1; {y decreases}
  {Now set x-increment}
  If x1 <= x2
    then b := 1 {x increases}
    else b := -1; {x decreases}
  {Initialize decision function and its deltas}

```

(continued)

The Toshiba P351 printer. The ultimate in 3-in-One™ technology.

The perfect business printer. Engineered to combine letter-quality printing, superb graphics and reliability with high speed. Plus a long list of sophisticated features. So you get three printers for the price of one.

Speed: 100 characters per second — letter quality; 288 characters per second (12 cpi) — draft quality.

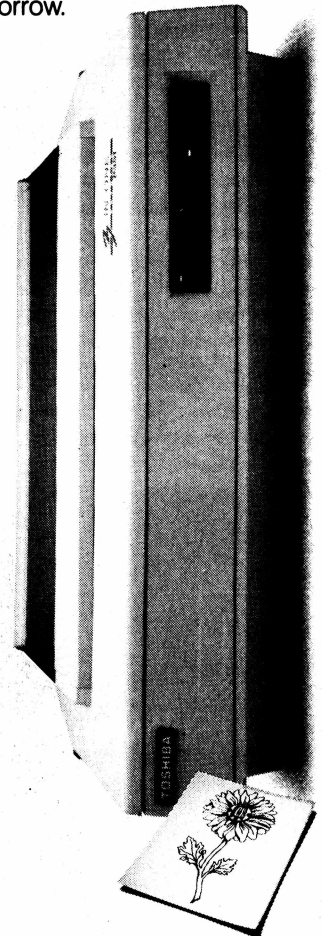
Dual Emulation: Qume Sprint II and IBM Graphics Printer (standard).

Reliability: In-use tests show the Toshiba 3-in-One printer can operate without fail for up to 7.7 years of normal workdays.

Durability: The 24-pin printhead lasts twice as long as nearest competitors.

Compatibility: Toshiba's 3-in-One printers are compatible with major software packages.

Interchangeability: Our parallel and serial interfaces make the 3-in-One series compatible with all micros. Today — and tomorrow.



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```

deltap := dx + dx;
d      := deltap - dy;
deltaq := d - dy;
{Locate and plot points}
Pset(x,y,1); {First point}
while y <> z do begin
  y := y + a;
  if d < 0
  then d := d + deltap
  else begin
    x := x + b;
    d := d + deltaq;
  end; {else}
  Pset(x,y,1);
end {while}
end {else}
end; {Pixel_line}

```

changes only about 1.5 dots per change in x —hardly visible at over 200 dots per inch.)

Second, this point-by-point calculation takes time. Even when the curve is smooth or nearly straight, every point must be calculated. For curves from simple functions this doesn't produce too much overhead, but for complicated mathematical equations or for curves produced by rotating images, this "overcalculation" is unacceptably slow.

The solution to both of these problems is to compute fewer points and to join the points computed with simple, easy-to-calculate curves. For most purposes these simple curves can be taken to be straight lines. If you only compute every fifth point and you connect the points by lines, there is a considerable time savings if point computations are reasonably complex and the line-drawing algorithm is fast. Furthermore, this solves the problem of gaps, since, in the example above, the points (1,5) and (2,10) would be joined by a small line segment "filling in" the missing four points.

The problem, then, is finding a fast line-drawing algorithm. Trying to find the equation of the line joining two points and then plotting it requires a considerable amount of real-number (decimal) arithmetic. This kind of arithmetic, especially multiplication and division, is quite slow in com-

parison with whole-number manipulation. Furthermore, since the coordinates of points on the screen (or printer page) are always integers—column and row numbers—you would naturally hope for a whole-number algorithm. Fortunately, there is one, called the Bresenham Line Algorithm (named for its inventor, J. E. Bresenham). It not only computes the points on the line connecting any two screen points, using whole-number arithmetic, but it accomplishes this feat *without using either multiplication or division!* Listing 4 contains a Pascal implementation of it. The procedure call is `Pixel_line(x1,y1,x2,y2,color)` where $x1,y1$ and $x2,y2$ are the endpoints of the line. For an easy-to-read description of the theory behind `Pixel_line`, see *Fundamentals of Interactive Computer Graphics* by James D. Foley and Andries Van Dam (Addison-Wesley, 1982).

Sometimes, when speed is even more important and points are very time-consuming to compute, you must cut down radically on the number of points calculated. Joining the points by straight lines will usually produce a figure that is too polygonal in appearance. In figure 1, the points are joined by curved pieces called *splines*, for which there are now very fast computational algorithms. There is some discussion of splines in Foley and Van Dam's book, but the

(continued)

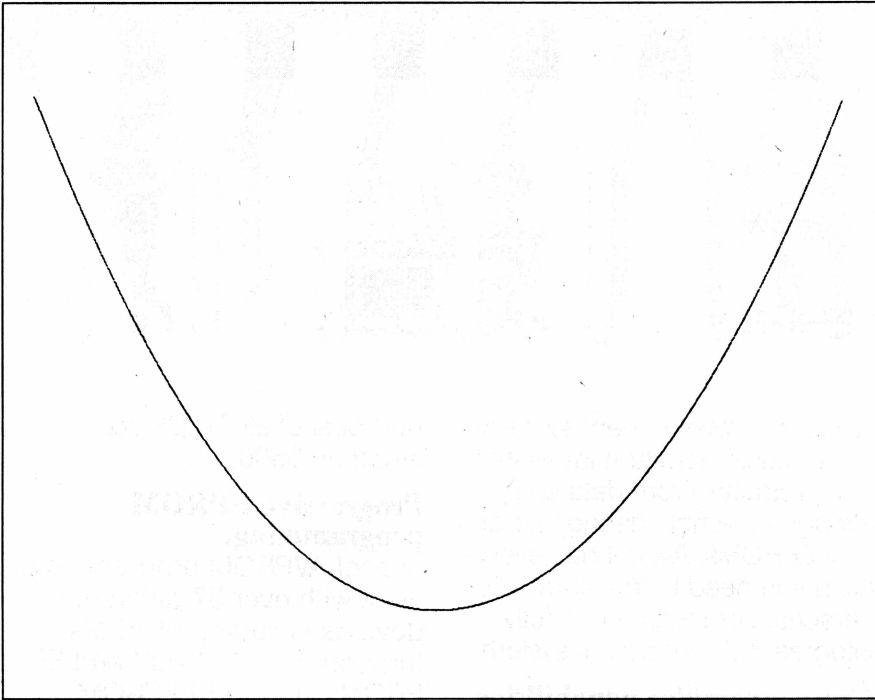


Figure 1: High-resolution plot of a parabola ($y = x*x$) created on an Epson FX-80 printer.

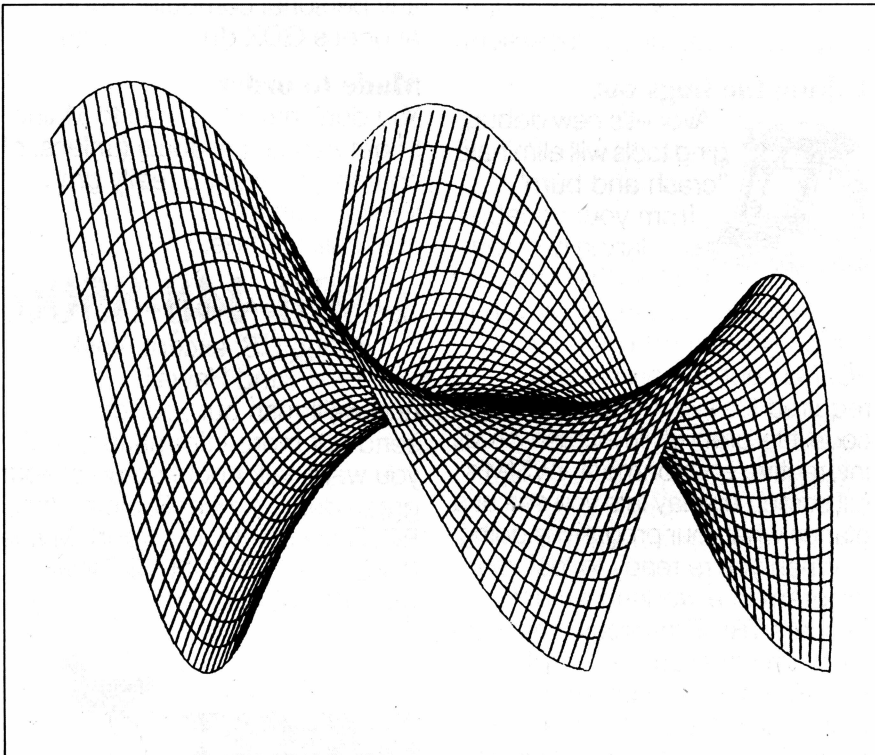


Figure 2: High-resolution plot of the surface $z = x^3 - 3xy^2$ (1600 by 640 dots prepared using the Epson FX-80 printer and the Bridge Software Math Utilities).

There are clever ways of getting even more speed out of the line drawing—especially for lines of small slope—by exploiting block moves of bytes.

most efficient algorithms are to be found in the current technical computer science journals.

FURTHER APPLICATIONS AND EXTENSIONS

Armed with procedures for drawing points and lines on the screen and on the printer, you can implement procedures for making very complex high-resolution pictures. It is possible, given enough memory, to set aside more pairs of arrays to increase further the image size you can print. This is the reason to use dynamic variables, the ones with the `^^`.

It is also possible to print your picture sideways, but this requires a restructuring of the procedure `Change` so that it addresses the points correctly.

Finally, you can use pixel masks to draw points on the graphics screen as well as the printer. The point and line-drawing procedures included in BASIC and Turbo Pascal, for example, are implemented by combining color and monochrome pixel masks with some version of Bresenham line drawing. There are clever ways of getting even more speed out of the line drawing—especially for lines of small slope—by exploiting *block* moves of bytes.

Figure 2 shows a surface plotted by an Epson FX-80 printer with a resolution of 1600 by 640 dots. It indicates the complexity of drawing possible with this method of printer addressing. ■